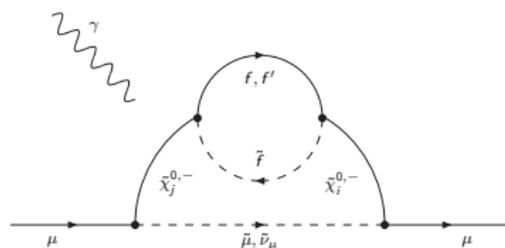


Magnetic moment $(g - 2)_\mu$ and beyond the Standard Model

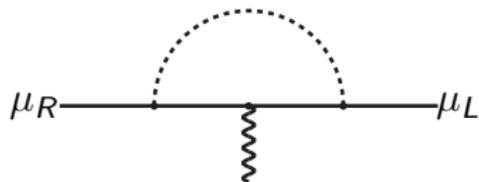
Dominik Stöckinger

TU Dresden



Collaboration Meeting, Seattle, July 2015

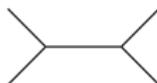
Why is a_μ special?



CP- and Flavour-conserving, chirality-flipping, loop-induced

compare: EDMs, $b \rightarrow s\gamma$
 $B \rightarrow \tau\nu$
 $\mu \rightarrow e\gamma$

EWPO



Outline

- 1 Isn't New Physics ruled out by LHC? Still motivated?
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Outline

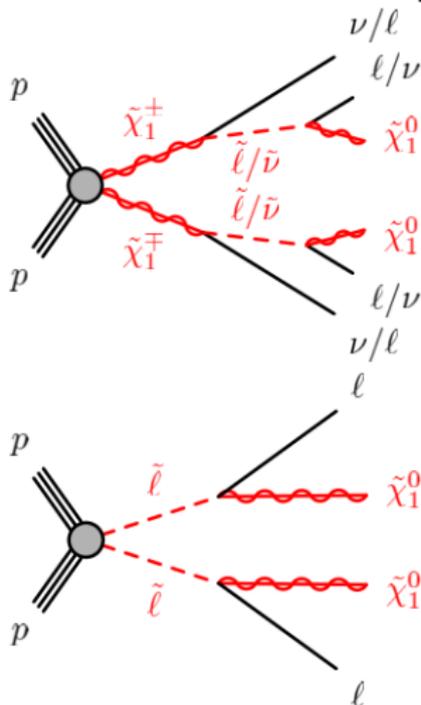
- 1 Isn't New Physics ruled out by LHC? Still motivated?

Beware of “propaganda plots”

Exclusion by LHC-data/EDMs/LFV
depends on assumptions!

Why isn't new physics ruled out by LHC?

Indeed, robust bounds on new coloured particles with simple decays, also on Z' with SM-like couplings

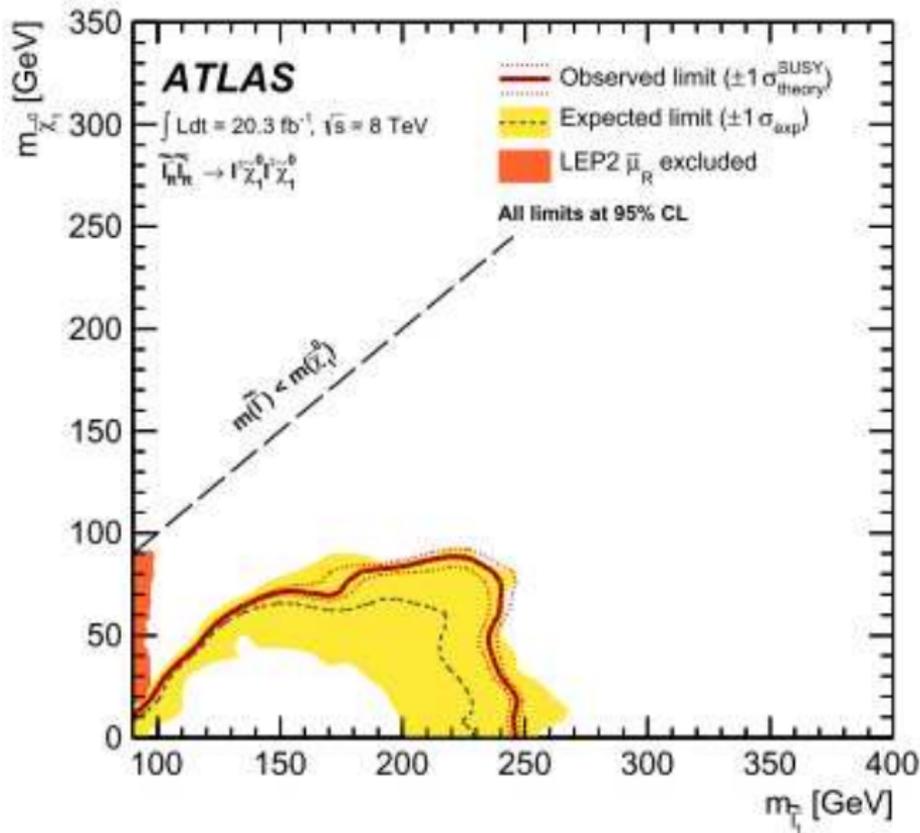


- But consider e.g. sleptons, charginos, neutralinos
- very low $\sigma \Rightarrow$ low mass reach

$$\sigma_{\text{LHC8}}(m_{\tilde{l}_R} = 370\text{GeV}) = 0.2\text{fb}$$

$$\sigma_{\text{LHC8}}(m_{\tilde{\chi}^\pm} = 450\text{GeV}) = 10\text{fb}$$

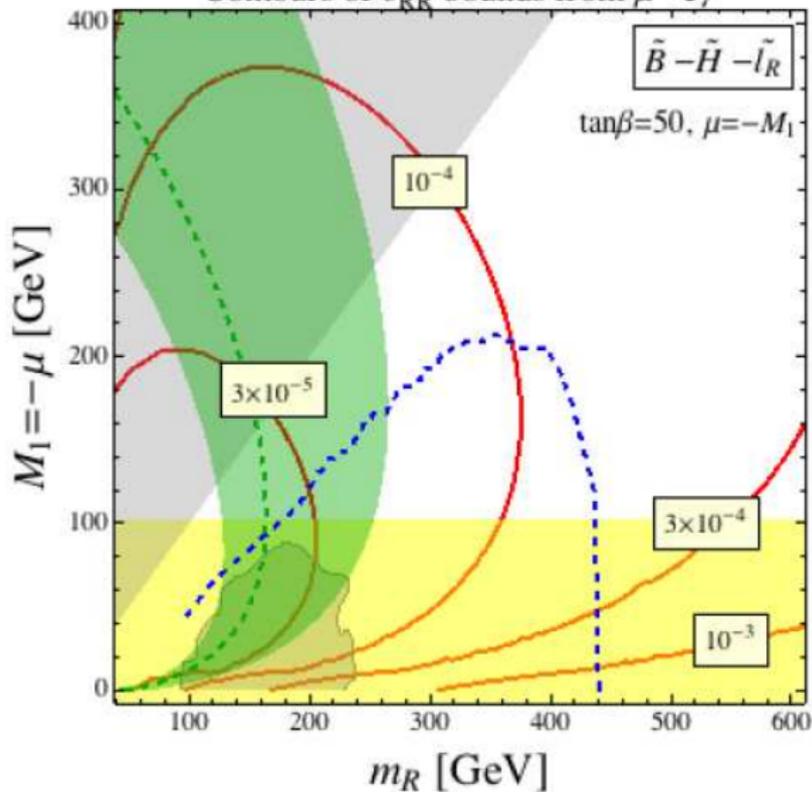
- analysis needs visible, hard leptons \Rightarrow simple decays and large mass splittings
- bad but possible in reality:
 $\chi_2^0 \rightarrow \chi_1^0 + H, H \rightarrow b\bar{b}$ essentially invisible



- ATLAS \tilde{l}_R search, assuming only two new particles,
- decay $\tilde{l}_R \rightarrow l \tilde{\chi}_1^0$
- σ is very low
- no exclusion above 250 GeV
- no exclusion if mass gap $\tilde{l}_R - \tilde{\chi}_1^0 < 80$ GeV

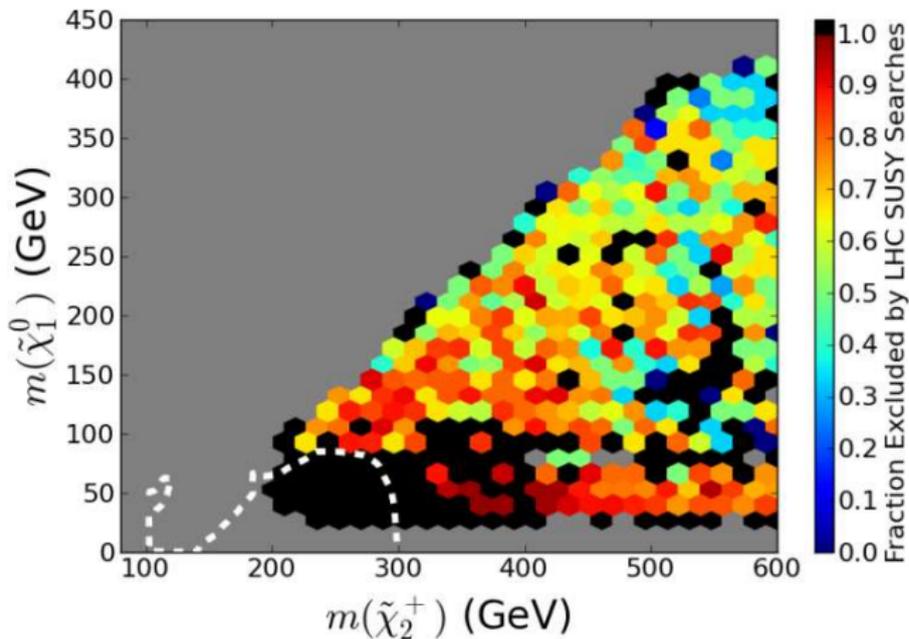
[arxiv:1403.5294]

Contours of δ_{RR}^{21} bounds from $\mu \rightarrow e\gamma$



- now three particles, $\tilde{l}_R, \tilde{B}, \tilde{H}$
- current LHC exclusion covers only masses below 250 GeV and mass gaps above 80 GeV
- even future LHC exclusion only twice as high
- Compare: [Fargnoli, Griendiger, Passehr, DS, Stöckinger-Kim '13] motivated BM4: $\mu = -160, M_1 = 140, m_{\tilde{\mu}_R} = 200, M_2 = m_{\tilde{\mu}_L} = 2000\text{GeV}, \tan\beta = 50$
this will remain allowed

[Calibbi, Galon, Masiero, Paradisi, Shadmi, arxiv:1502.07753]



- SUSY models with “low fine tuning”
 $\tilde{t} > \tilde{l} > \chi^{\tilde{0},\pm}$
- only small region is completely excluded
- all neutralinos and charginos can be light

[Cahill-Rowley, Hewett, Ismail, Rizzo, arxiv:1407.4130]

Hence new physics is still possible!

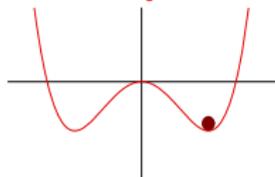
- in particular, new particles can still give large a_μ
- however, it is true that some scenarios are excluded, and specific (sometimes non-traditional) scenarios are now better motivated (e.g. very large or very small mass splittings)

similar for other observables:

- $B_s \rightarrow \mu\mu$ rules out SUSY with very large $\tan\beta$ and small CP-odd Higgs mass
- EDMs rule out new physics with small masses and large complex phases

Why new physics?

Big questions... point to (TeV scale) new physics



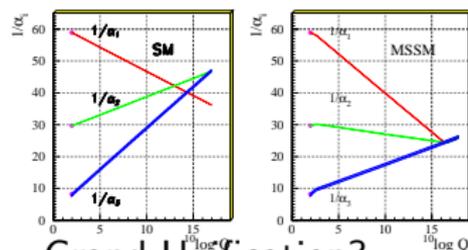
EWSB, Higgs, scalar particle?

hierarchy M_{Pl}/M_W ? Naturalness?



Dark Matter?

Baryon Asymmetry?



Grand Unification?

Flavor Structure?

Many ideas for new fundamental theories, principles, interactions

Need complementary experiments to discover and scrutinize new physics

Outline

2 Overview: New Physics in General

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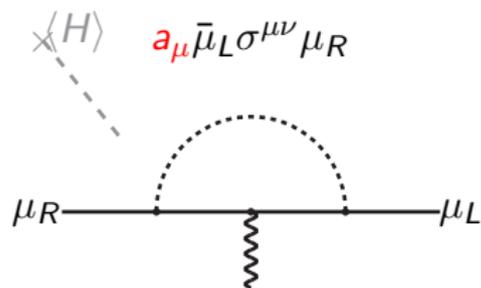
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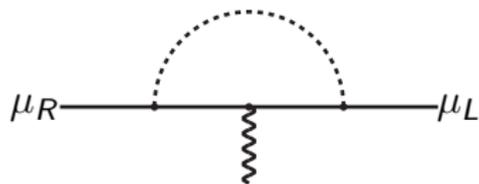
Explain new physics contributions to a_μ

Loop contributions to a_μ , m_μ related to **source of chirality flips**



Very different contributions to a_μ : classify $\propto C$

$$\mathcal{O}(C) \left(\frac{m_\mu}{M}\right)^2$$



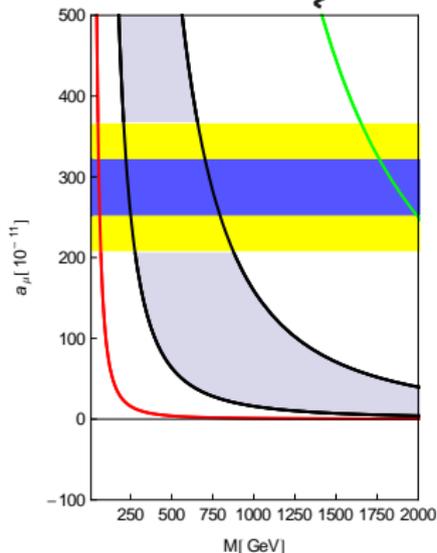
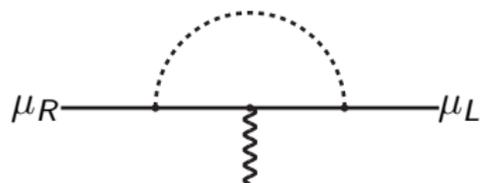
$$C = \frac{\delta m_\mu(\text{N.P.})}{m_\mu}$$



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$\mathcal{O}(1)$

$\mathcal{O}\left(\frac{\alpha}{4\pi} \dots\right)$

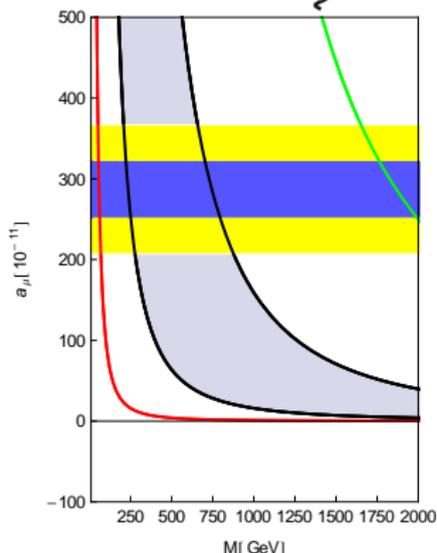
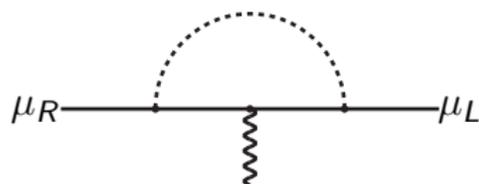
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$Z', W', \text{UED, Littlest Higgs (LHT)} \dots$

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supersymmetry ($\tan \beta$), unparticles

[Cheung, Keung, Yuan '07]

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extra dim. (ADD/RS) (n_c)...

[Davioudasl, Hewett, Rizzo '00]

[Graesser, '00][Park et al '01][Kim et al '01]

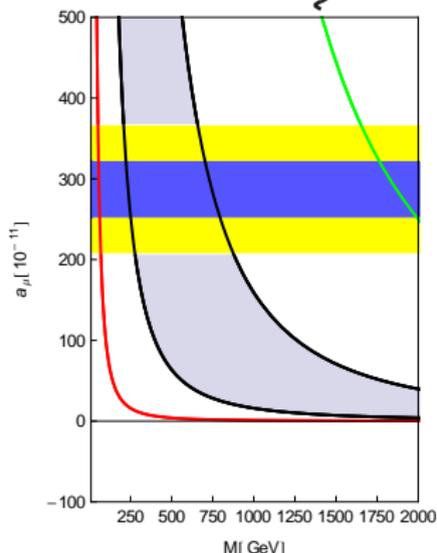
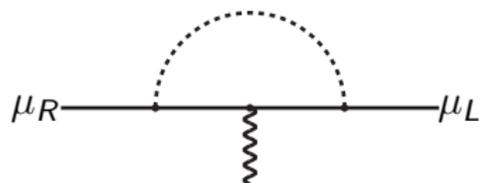
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[Czarnecki, Marciano '01]

[Crivellin, Girschbach, Nierste '11][Dobrescu, Fox '10]

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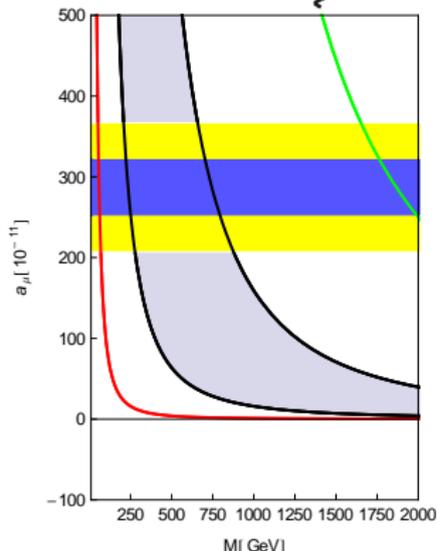
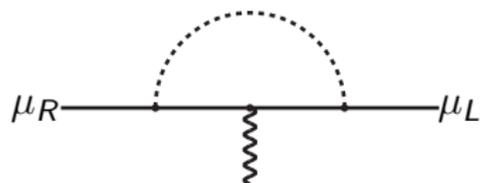
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$\ll \frac{\alpha}{4\pi}$

dark photon ...

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Navigate through examples

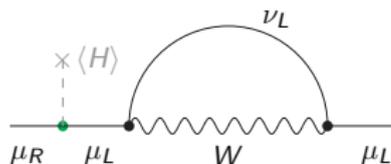
- SM weak

- \leq two new particles (structure as for SM weak, easy to estimate)

- \geq three new particles

Navigate through examples

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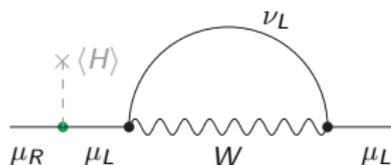


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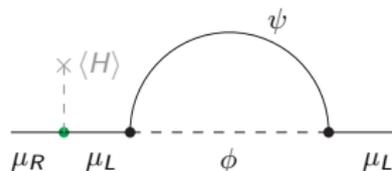
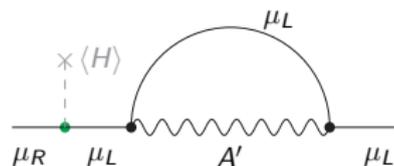
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Navigate through examples

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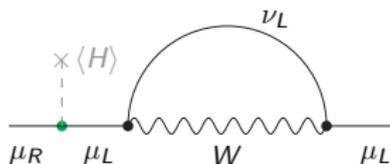
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model-“independent” study [Freitas, Kell, Lykken, Westhoff '14] and other models



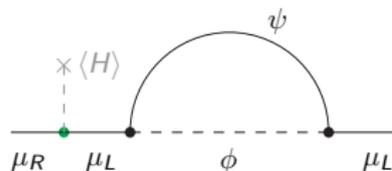
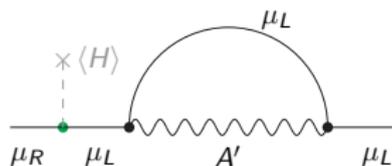
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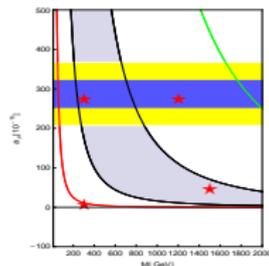
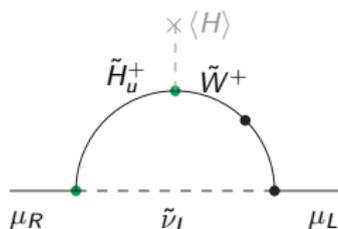
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- \geq three new particles \Rightarrow (ab)use SUSY-scenarios as simplified models

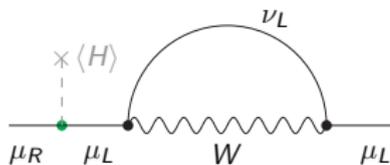


Model-''independent'' analysis of \leq two new fields

[Freitas, Kell,
Lykken,
Westhoff '14]

- SM: doublet $L = \begin{pmatrix} \nu_L \\ \mu_L \end{pmatrix}$, singlet μ_R , doublet H

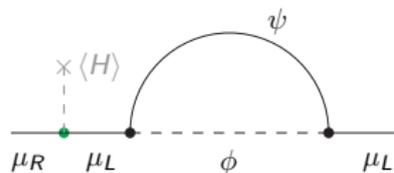
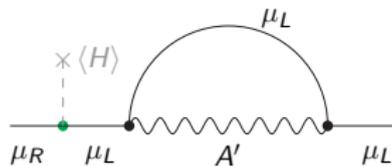
Chirality flip: $\bar{L}H\mu_R \rightarrow \langle H \rangle \bar{\mu}_L\mu_R$



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- New fields: either doublets, singlets or triplets, no flavour violation

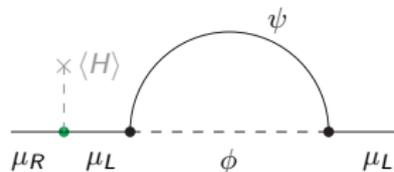
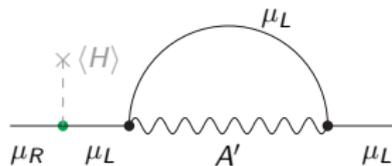


\Rightarrow no additional chirality flip! Behaviour like $a_{\mu}^{\text{SM, weak}}$

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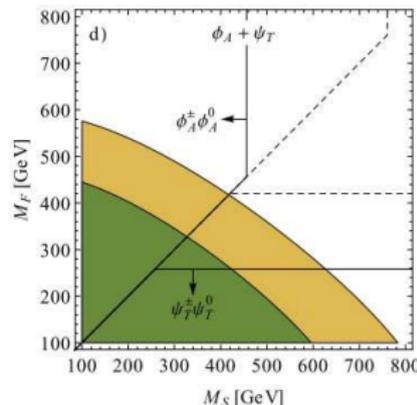
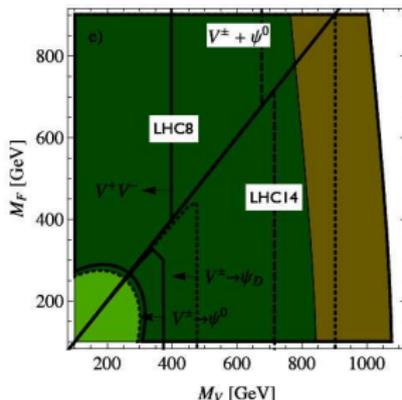
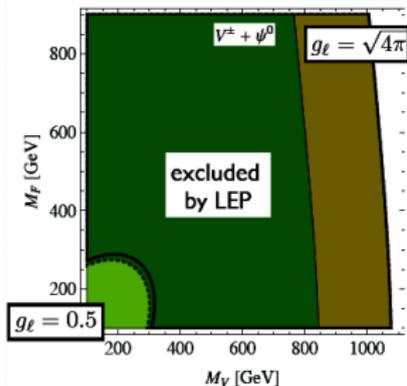
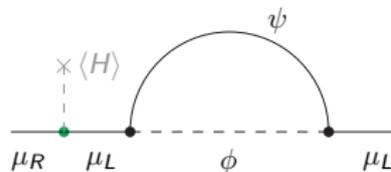
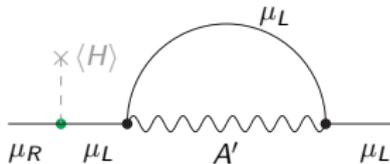
\Rightarrow no additional chirality flip! Behaviour like $a_{\mu}^{\text{SM, weak}}$

- large contributions need $M < \mathcal{O}(500)$ GeV and $g_{\text{New}} = \mathcal{O}(1)$
- Constrained by LHC and LEP

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[Freitas, Kell, Lykken, Westhoff '14]

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Some scenarios still viable, will be tested at LHC14

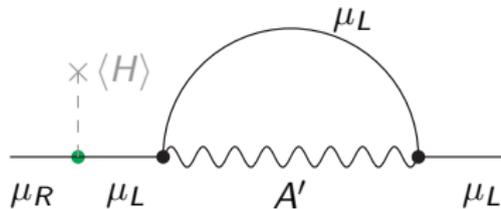
Beware of “model-independent” statements

What about dark photons?

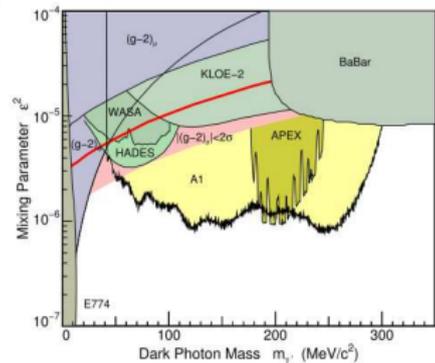
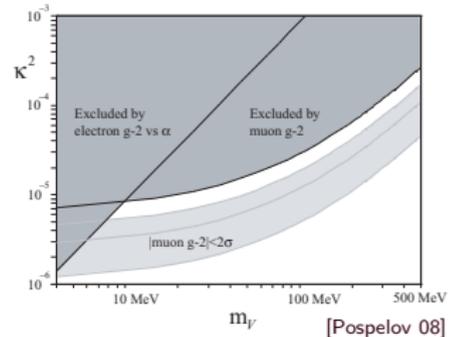
What about two-Higgs doublet model?

Dark photon: “second most promising scenario” [Marciano]

- very light/weakly interacting \Rightarrow not covered by previous analysis



- theory motivation: new U(1) gauge group (from GUTs, ...)
- **could explain:** dark matter, $(g - 2)_\mu$ (for very specific coupling/mass range)
- a_μ -explanation now almost completely excluded!!
- generalization: “dark Z” with more general couplings, also strongly constrained



[A1/Mainz '14]

[Davoudiasl, Lee, Marciano '14][Izaguirre et al '13]

Two-Higgs Doublet Model: one field but tricky behaviour

- Second Higgs doublet well motivated in theory
- Promising case: H_1 couples to leptons, $H_2 \approx H_{SM}$ to quarks (type X)

recent analyses: [Broggio, Chun, Passera, Patel, Vempati '14, Ilisie '15]

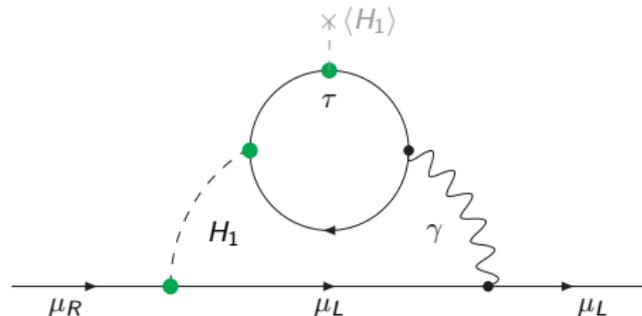
- Not covered in previous analysis for two reasons:
 - 1 no fields with vacuum expectation value
 - 2 only one-loop contributions to a_μ

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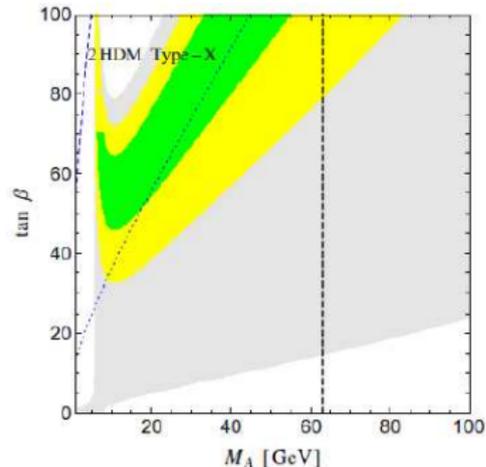
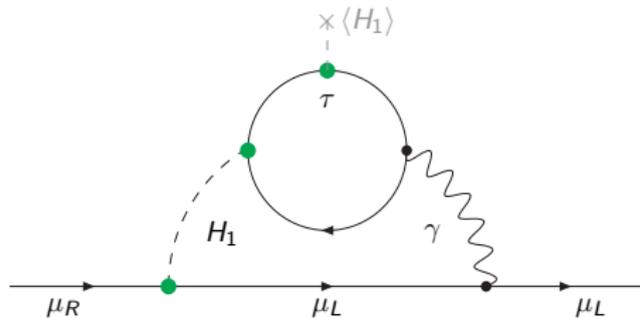


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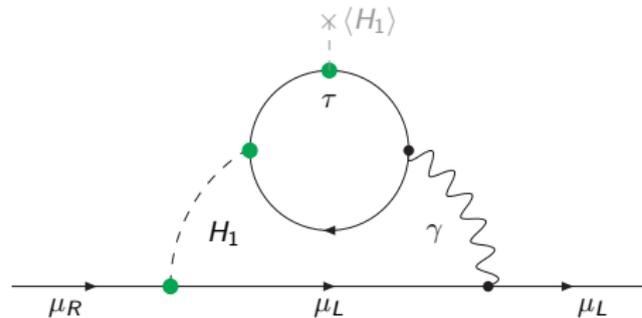


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$$\propto \frac{y_\mu y_\tau m_\tau}{M_{H_1}^2} \approx \frac{\tan^2 \beta y_{\mu,\text{SM}}^2 m_\tau}{M_{H_1}^2}$$

explanation:

$$\tan \beta = \frac{\langle H_2 \rangle}{\langle H_1 \rangle} \approx \frac{\langle H_{\text{SM}} \rangle}{\langle H_1 \rangle} \gg 1$$

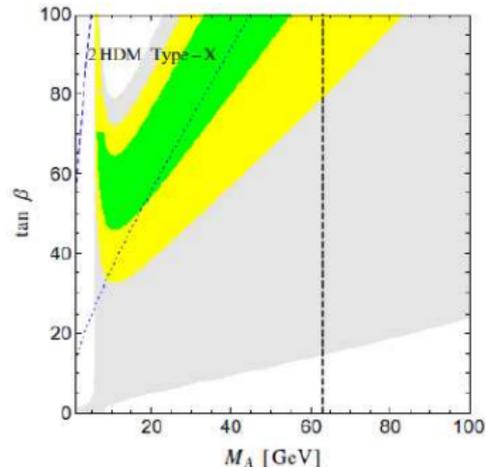
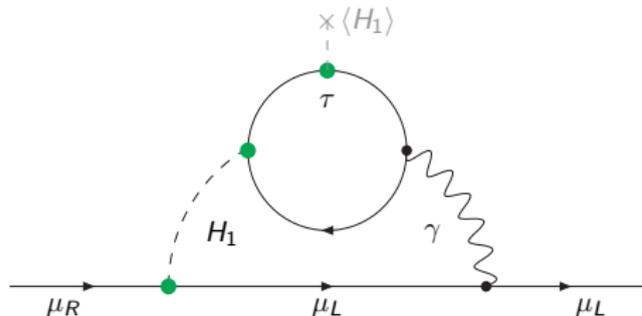
$$y_{\mu,\tau} = \frac{m_{\mu,\tau}}{\langle H_1 \rangle} \approx \tan \beta y_{\mu,\tau,\text{SM}}$$

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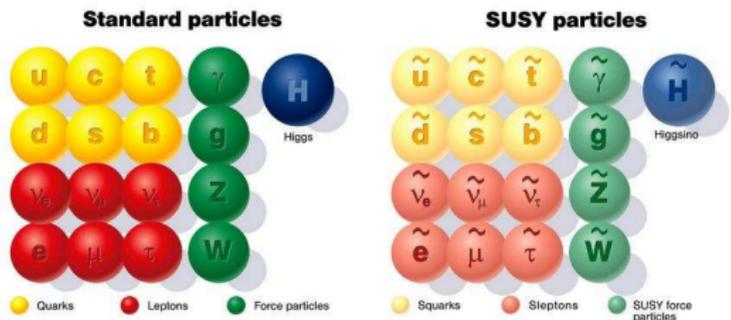
Viable region $M_A \sim 50$ GeV, $\tan \beta \sim 100$ not excluded by anything

Models with \leq two new fields already rich:
light or heavy new particles, constrained/testable by LHC and/or
low-energy data

further models: Z' with $L_\mu - L_\tau$, dark Z (mass mixing), non-MFV models

SUSY and the MSSM — four examples

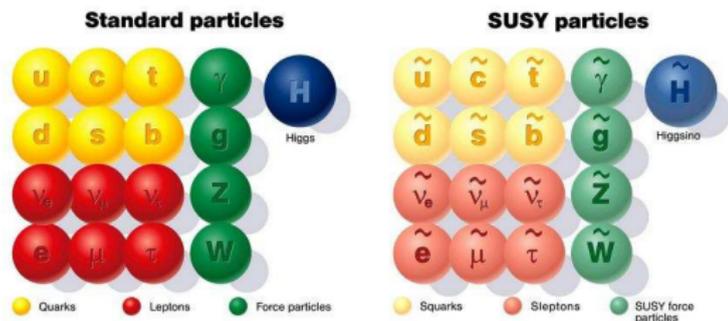
- MSSM:



- free parameters: \tilde{p} masses and mixings, μ and $\tan \beta$

SUSY and the MSSM — four examples

- MSSM:



- free parameters: \tilde{p} masses and mixings, μ and $\tan \beta$

$$a_\mu^{\text{SUSY}} \approx 12 \times 10^{-10} \tan \beta \text{ sign}(\mu) \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

SUSY could be the origin of the observed $(30 \pm 8) \times 10^{-10}$ deviation!

Chirality flip and $\tan \beta$ -enhancement

Two Higgs and Higgsino doublets:

$$\tan \beta = \frac{\langle H_u \rangle}{\langle H_d \rangle}, \quad \mu = H_u - H_d \text{ transition}$$

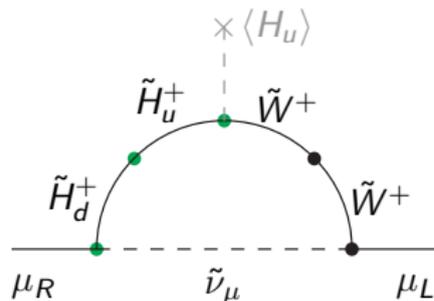
Large Yukawa as in 2HDM

$$m_\mu^{\text{tree}} = y_\mu \langle H_d \rangle$$

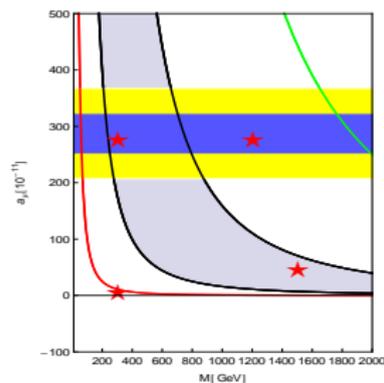
Diagram enhanced by Yukawa and large “other” vev

$$\propto y_\mu \langle H_u \rangle \mu = m_\mu \tan \beta \mu \quad \rightarrow a_\mu^{\text{SUSY}} \propto \tan \beta \text{sign}(\mu) \frac{m_\mu^2}{M_{\text{SUSY}}^2}$$

enhancement $\propto \tan \beta = 1 \dots 50$ (and $\propto \text{sign}(\mu)$)



1st example: large masses, small a_μ
Obviously, the LHC rules out specific SUSY models as explanations of g-2. Consider one of them, the “Constrained MSSM”.



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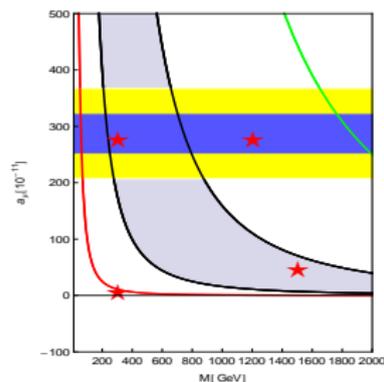
Assumption at GUT scale:

m_0 = universal scalar mass

$m_{1/2}$ = universal fermion mass

α = universal gauge coupling

⇒ physical masses strongly correlated



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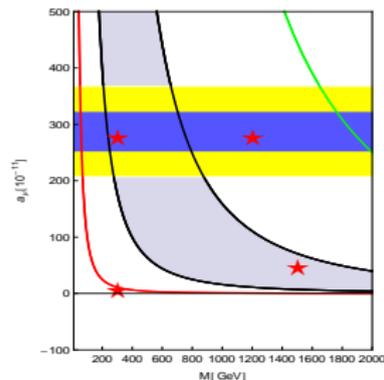
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- Observed Higgs mass
needs very heavy stops
⇒ all new scalars heavy (multi-TeV)
- LHC requires heavy gluinos
⇒ all new fermions heavy
- hence, a_μ contributions negligible

1st example: large masses, small a_μ

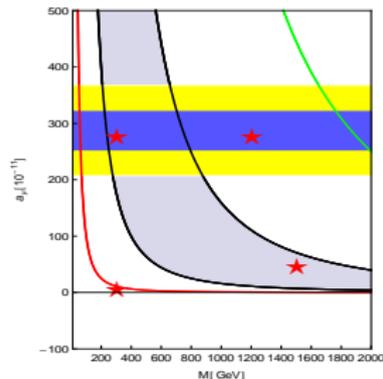
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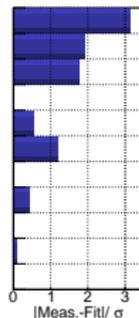


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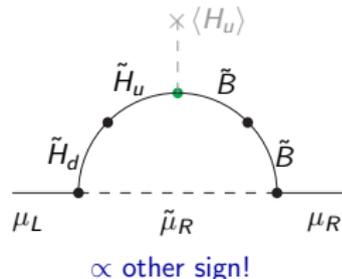
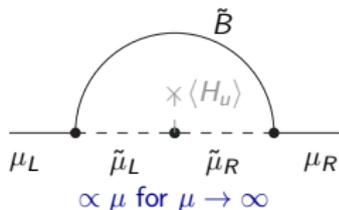
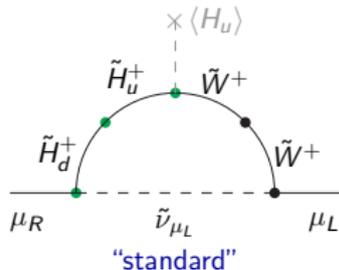
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	CMSSM, LHC, $m_h=126$ GeV	
$a_\mu - a_\mu^{\text{SM}}$	$(2.9 \pm 0.8 \pm 0.2)E-9$	0.3E-9
BR($b \rightarrow s\gamma$)	$(3.55 \pm 0.26 \pm 0.23)E-4$	2.88E-4
BR($B \rightarrow \tau\nu$)	$(1.67 \pm 0.39)E-4$	0.99E-4
BR($B_s \rightarrow \mu^+\mu^-$)	$<(4.50 \pm 0.30)E-9$	3.61E-9
Δm_s (ps^{-1})	$17.78 \pm 0.12 \pm 5.20$	20.58
$\sin^2\theta_{\text{eff}}^l$	0.23113 ± 0.00021	0.23138
m_W (GeV)	$80.385 \pm 0.015 \pm 0.010$	80.386
m_h (GeV)	$126.0 \pm 2.0 \pm 3.0$	124.4
LHC		
$\Omega_{\text{CDM}} h^2$	$0.1123 \pm 0.0035 \pm 0.0112$	0.1112
σ^{SI} (pb)		2.44E-11



2nd example: small masses, large a_μ



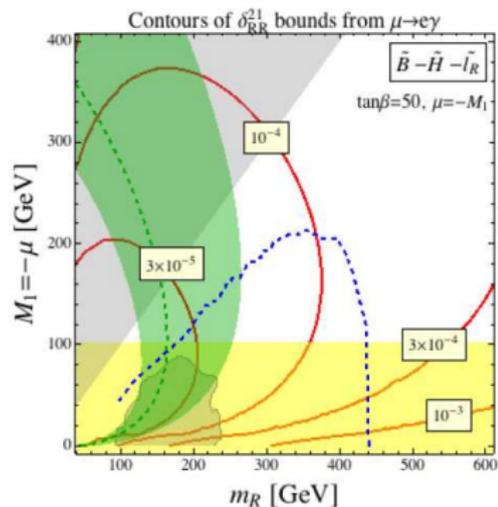
- large a_μ for $m_{\text{weak}} \sim 100 \dots 400$ GeV

[Fargnoli, Gnendiger, Passehr, DS, Stöckinger-Kim '13]

- evade LHC by $m_{\text{coloured}} \gg 1$ TeV
- can carry out dedicated LHC studies and top-down motivation

[Endo; Yanagida; Roy; Calibbi; Roszkowski...]

- such scenarios are viable, some might even survive LHC14



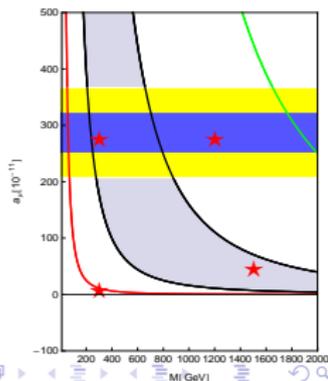
Comments:

- CMSSM assumptions are simple but theoretically not preferred
- CMSSM (and other models) cannot explain large a_μ any more
- Now: theory as well as experiment motivates to construct models with more complicated mass relations, e.g. higher mass splittings

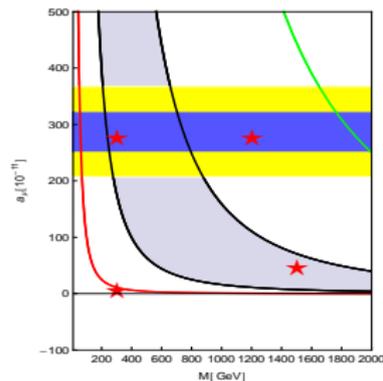
many model building studies [Endo, Hamaguchi, Ibe, Yanagida, D.P. Roy, et al]

- Light particles are (and will remain) possible but specific models will be tested at LHC14, particular if they should also explain dark matter

[Kowalska, Roszkowski, Sessolo, Williams '15]



3rd Example: large a_μ for large masses



Is it possible to explain the a_μ deviation with **TeV-scale SUSY**?

What is the largest possible SUSY contribution to a_μ ?

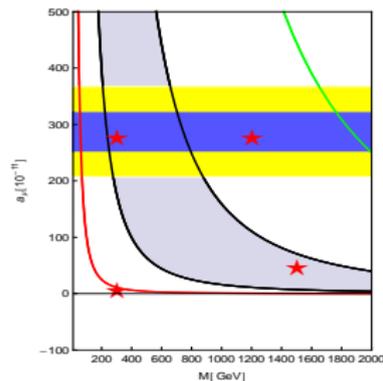
3rd Example: large a_μ for large masses

Idea: radiative muon mass in SUSY

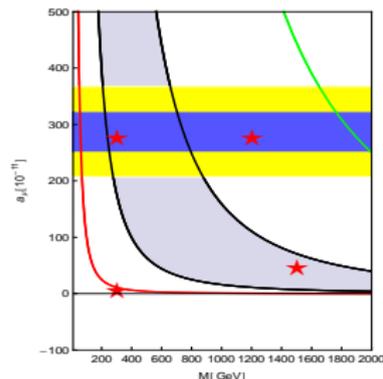
$$m_\mu^{\text{tree}} = y_\mu v_d$$

set $v_d \rightarrow 0$, $\tan \beta \rightarrow \infty$

[Dobrescu, Fox '10][Altmannshofer, Straub '10] (see also [Davies, March-russell, Mccullough '11])



3rd Example: large a_μ for large masses



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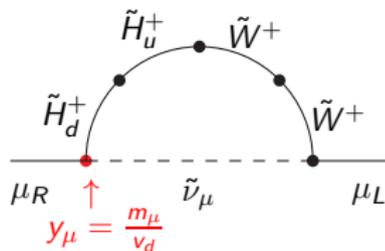
[Dobrescu, Fox '10][Altmannshofer, Straub '10] (see also [Davies, March-russell, Mccullough '11])

- MSSM-scenarios for $\tan \beta \rightarrow \infty$ can be regarded as genuinely interesting parameter regions or as simplified models which realize radiative muon mass generation

Large a_μ in MSSM for $\tan \beta \rightarrow \infty$

[Bach, Park, DS, Stöckinger-Kim, '15]

“standard case” (equal masses, 1-loop)



$$a_\mu^{\text{SUSY}} \approx 12 \times 10^{-10} \tan \beta \text{ sign}(\mu) \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

Large a_μ in MSSM for $\tan \beta \rightarrow \infty$

[Bach, Park, DS, Stöckinger-Kim, '15]

actually, including higher order effects

[Marchetti, Mertens, Nierste, DS '08]

$$y_\mu \approx \frac{m_\mu}{v_d + v_u (1\text{-loop})} = \frac{y_\mu^{\text{tree}}}{(1 + \Delta_\mu)}$$

$$a_\mu^{\text{SUSY}} \approx \frac{12 \times 10^{-10} \tan \beta \text{ sign}(\mu)}{1 - 0.0018 \tan \beta \text{ sign}(\mu)} \left(\frac{100 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

Large a_μ in MSSM for $\tan \beta \rightarrow \infty$

limit $\tan \beta \rightarrow \infty$

$$a_\mu^{\text{SUSY}} \approx -70 \times 10^{-10} \left(\frac{1000 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

$\tan \beta$ and $\text{sign}(\mu)$ drop out, large contributions for $M_{\text{SUSY}} \sim \text{TeV}$!

Large a_μ in MSSM for $\tan \beta \rightarrow \infty$

limit $\tan \beta \rightarrow \infty$

$$a_\mu^{\text{SUSY}} \approx -70 \times 10^{-10} \left(\frac{1000 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

“standard” case: sign wrong!

Large a_μ in MSSM for $\tan \beta \rightarrow \infty$

limit $\tan \beta \rightarrow \infty$

$$a_\mu^{\text{SUSY}} \approx +37 \times 10^{-10} \left(\frac{1000 \text{ GeV}}{M_{\text{SUSY}}} \right)^2$$

sign positive e.g. if $|\mu| \gg M_{\text{SUSY}}$ (then only $\tilde{B}\tilde{\mu}_L\tilde{\mu}_R$ important)

Sample TeV-scale masses:

μ	M_1	M_2	m_L	m_R	$a_\mu/10^{-9}$
15	1	-1	1	1	3.01
1.3	1.3	-1.3	26	1.3	2.90

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\exists models with large a_μ in spite of TeV-scale masses

[also other models with radiative muon mass [Crivellin et al, Straub et al...]]

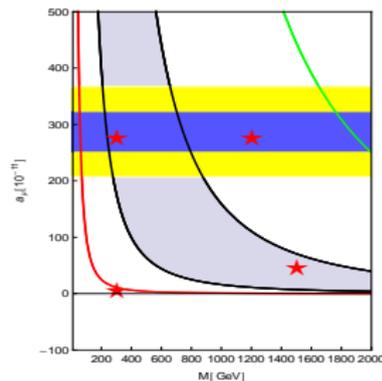
not easy to detect at LHC, but large couplings \Rightarrow other effects

4th Example: small a_μ , small masses

Questions:

Can all SUSY scenarios give **large contributions**?

What is the SUSY contribution with R-symmetry?



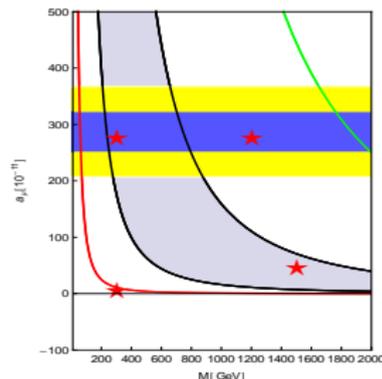
4th Example: small a_μ , small masses

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- Opposite reaction to LHC: not less, but **more SUSY, more symmetry, more light particles!**
- possible with R-symmetry, MRSSM [Kribs, Poppitz, Weiner '08]
- particles charged under conserved R-charge
- gauge bosons have two gauginos ($R = \pm 1$) and one scalar superpartner
- R-symmetry suppresses LHC cross sections, lighter particles viable [Kribs, Martin '10]
- compatible with Higgs and LEP constraints [Diessner, Kalinowski, Kotlarski, DS '14]



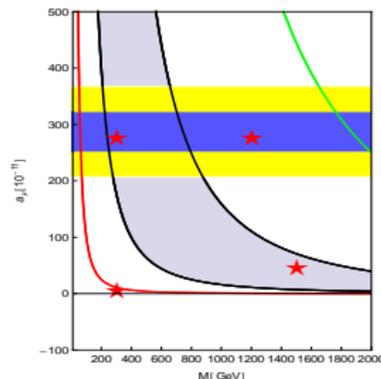
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- kills $g - 2$ (no $\tan \beta$ enhancement)
- all $\tan \beta$ -enhanced contributions: $\propto \mu M_{1,2}$
- both μ and Majorana gaugino masses forbidden by R-symmetry
predictive!



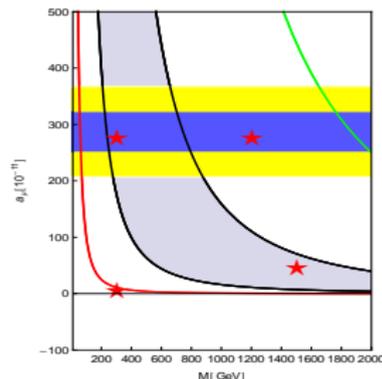
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\exists well-motivated models which predict \approx zero a_μ

[other models: LHT, UED, Z'...]

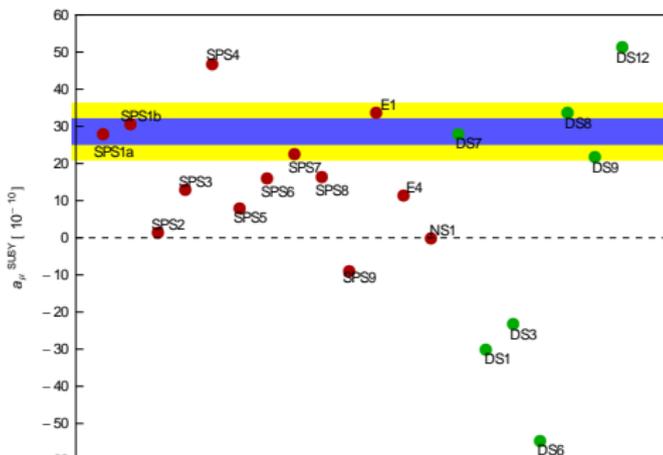
will be under pressure if non-zero a_μ is confirmed

Using a_μ : complementarity to LHC

Many different models with different contributions to a_μ



New measurement will be very important

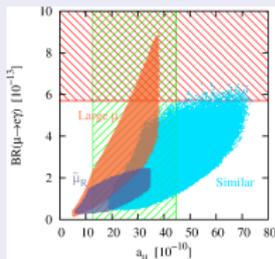
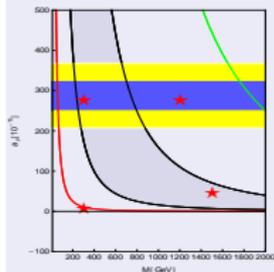


SPS benchmark points
[v.Weitershausen,Schäfer,
Stöckinger-Kim,DS '10]

LHC Inverse Problem (300fb^{-1})
can't be distinguished at LHC
[Sfitter: Adam, Kneur, Lafaye,
Plehn, Rauch, Zerwas '10]

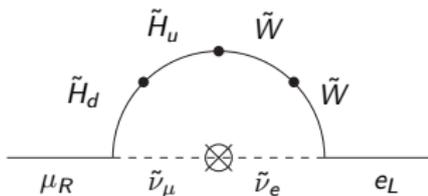
- a_μ distinguishes models
- helps measure parameters

Complementarity/correlation with $\mu \rightarrow e\gamma$

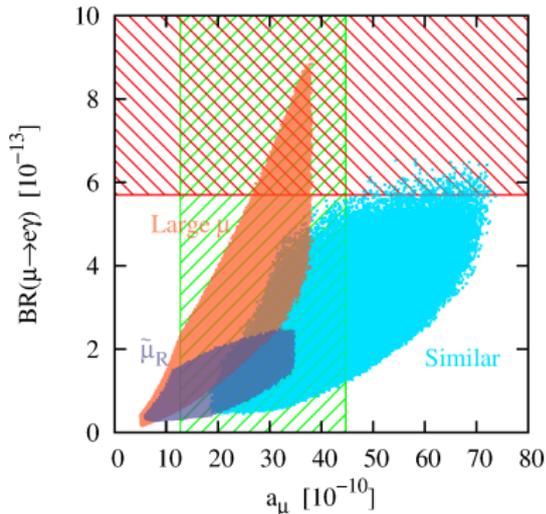


LHC $\oplus a_\mu$: masses and model details

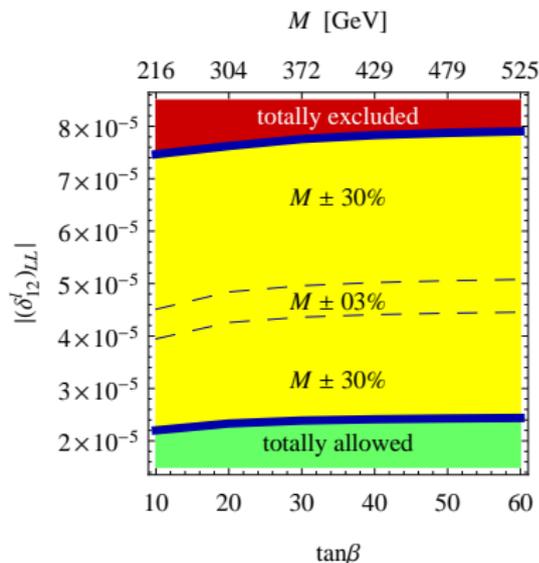
LFV $\oplus a_\mu$: LFV parameters



$\mu \rightarrow e\gamma$: correlation with $g - 2$ depends on scenario



parameter regions where single diagrams dominate



bounds on δ_{LL} assuming M is fixed to accommodate a_μ

- study correlation for fixed $\delta_{LL} = m_{L12}^2 / \sqrt{m_{L11}^2 m_{L22}^2} = 2 \times 10^{-5}$
 - ▶ correlation often studied [Chacko, Kribs'01; Isidori, Mescia, Paradisi, Temes '07]
 - ▶ but depends on mass pattern [Kersten, Park, DS, Velasco-Sevilla '14]
- still, can constrain δ_{LL} assuming a_μ and mass pattern

Precision computations (our work and plans)

Precision computations in new physics models motivated

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Precision computations in new physics models motivated

- e.g. two-loop contributions qualitatively different
- reduce theory uncertainty (e.g. from $\alpha = 1/137$ or $\alpha = 1/128$)
- SUSY uncertainty $\sim 3 \times 10^{-10}$ [DS '06]

Status:

- SUSY: 8 of 9 classes of two-loop contributions known, rest in progress [65000 diagrams computed, 1 class of counterterms missing]
- 2HDM: leading two-loop contributions known, rest in progress

Outline

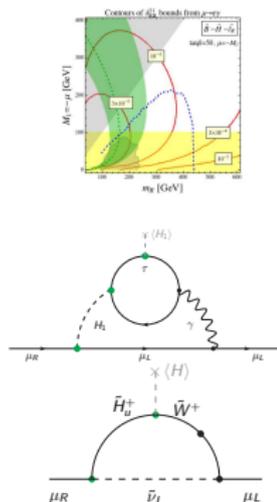
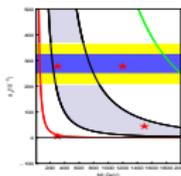
4 Conclusions

Summary: a_μ as a probe of new physics

- New physics not excluded and still well motivated

- $a_\mu^{\text{N.P., SUSY}}$ very model-dependent

- ▶ can be $\mathcal{O}(\pm 1 \dots 50) \times 10^{-10}$
- ▶ different mechanisms
- ▶ special SUSY scenarios
 $\tan \beta \rightarrow \infty$, R-symmetry



- New measurement will have strong impact

- ▶ constraints, model discriminator
- ▶ unique properties
- ▶ precise predictions (will be) available

